

# Biological Insights from a Simulation Model of the Critical FtsZ Accumulation Required for Prokaryotic Cell Division

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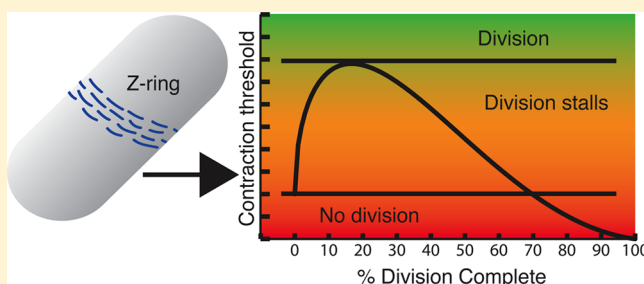
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**ABSTRACT:** A simulation model of prokaryotic Z-ring assembly, based on the observed behavior of FtsZ *in vitro* as well as on *in vivo* parameters, is used to integrate critical processes in cell division. According to the model, the cell's ability to divide depends on a "contraction parameter" ( $\chi$ ) that links the force of contraction to the dynamics of FtsZ. This parameter accurately predicts the outcome of division. Evaluating the GTP binding strength, the FtsZ polymerization rate, and the intrinsic GTP hydrolysis/dissociation activity, we find that inhibition of GTP–FtsZ binding is an inefficient antibacterial target. Furthermore, simulations indicate that the temperature sensitivity of the *ftsZ84* mutation arises from the conversion of FtsZ to a dual-specificity NTPase. Finally, the sensitivity to temperature of the rate of ATP hydrolysis, over the critical temperature range, leads us to conclude that the *ftsZ84* mutation affects the turnover rate of the Z-ring much less strongly than previously reported.



Cytokinesis is the final step in cell division, the process whereby the parent cell divides into two daughter cells each containing a complete copy of the genome. Although cytokinesis forms an attractive target for antibacterial drug design, success to date has been hampered by a lack of understanding of the interplay of the relevant factors. A key stage in prokaryotes is the formation of a contractile ring, composed of fibers of the cytoskeletal protein FtsZ, at the division plane.<sup>1</sup> This so-called Z-ring is anchored to the cytoplasmic face of the cell membrane by the direct interaction of FtsZ with the membrane-binding proteins ZipA and FtsA.<sup>2</sup> These proteins constitute the structural scaffold for the recruitment of various additional proteins to form the complete "divisome" complex, which includes the enzymes required for peptidoglycan synthesis and remodeling. Following assembly, the Z-ring contracts, drawing the membrane on opposite sides of the cell together. For recent reviews, see Typas et al.,<sup>3</sup> Egan and Vollmer,<sup>4</sup> and den Blaauwen.<sup>5</sup>

Despite extensive work since the discovery in 1991 that FtsZ is the major component of the contractile ring,<sup>6</sup> the mechanism driving the assembly and contraction of the Z-ring and the link between protein function and cellular phenotype remain poorly understood. Translation of the activity of FtsZ measured *in vitro* to its function *in vivo* is critical to further our understanding of cytokinesis.

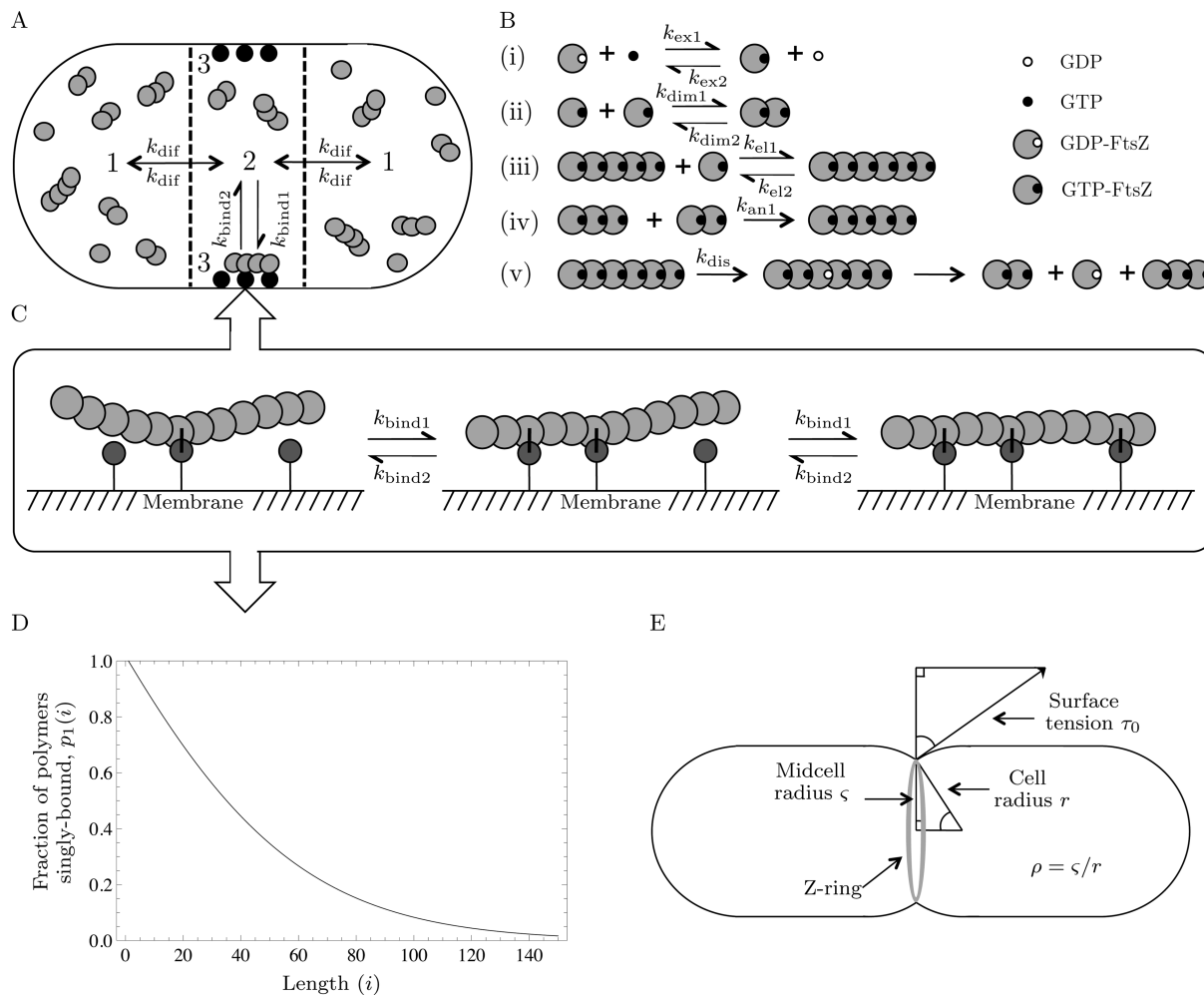
We have developed a model of this key phase of cell division<sup>7</sup> and showed that the results are consistent with the division behavior observed following the loss of expression of FtsA or

ZipA, two components of the *Escherichia coli* divisome complex. This strongly suggests that the simulation model is a reliable tool for probing the early stages of cytokinesis that critically depend on the Z-ring and its membrane interactions. Here we explore how different perturbations of the system, such as mutations, which are represented in the model as changes in various biochemical and biophysical parameters, affect the initiation and completion of cell division. In each case, the predictions correspond with observed phenomena (up to absolute magnitudes of time scales, as will be explained further below) and can be used to evaluate which components are likely to constitute effective drug targets. We refer to our model as CAM-FF (critical accumulation of membrane-bound FtsZ fibers). After summarizing the key aspects of the model, we review the wild-type behavior, which forms our reference point, followed by analysis of (1) a reduction in the measured rate of GTP hydrolysis by (a) a reduction in the intrinsic rate of GTP hydrolysis and/or dissociation, (b) a reduction in the GTP binding strength, and (c) a reduction in the FtsZ polymerization rate; (2) depletion or overexpression of anchor proteins; (3) overexpression of FtsZ; and (4) the *ftsZ84* mutant that has a significantly reduced FtsZ GTPase activity, combined with the

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**Figure 1.** Schematic diagram of the CAM-FF model. (A) The cell is conceptually divided into three compartments: (1) the cell caps, (2) the midcell, and (3) the midcell membrane. FtsZ moves between the cell caps and the midcell regions by diffusion. Exchange between the midcell region and the midcell membrane occurs upon interaction of FtsZ with membrane anchor sites and subsequent polymerization. (B) In the notation of Surotsev et al., the chemical reactions in our model are (i) nucleotide exchange, (ii) dimerization, (iii) elongation, (iv) annealing, and (v) polymer breakdown following GTP hydrolysis (steps i–iii are reversible, whereas steps iv and v are thought to be irreversible). (C) Depending on the anchor density, an FtsZ polymer may bind to one or more anchor sites. (D) Fraction of membrane-bound polymers expected to be attached by a single FtsZ–anchor interaction, as a function of polymer length for an anchor density  $P_a$  of 0.043 and an equilibrium constant  $\kappa$  of  $0.2 \mu\text{M}$ . (E) Z-Ring contraction pulls the membrane inward against the outward force from the surface tension generated at the inner membrane.

introduction of ATPase activity. Finally, we discuss the implications of our simulations for antibacterial agents.

### EXPERIMENTAL PROCEDURES

We develop and apply CAM-FF to a range of different bacteria whose cell division phenotype has yet to be explained. CAM-FF takes as its point of departure the “Z-centric hypothesis” (viz., assembly of the Z-ring and the force of its constriction originate from FtsZ) and extends earlier work by Surotsev et al.<sup>8</sup> Key assumptions are (i) the lack of dependence of Z-ring formation on the cyclization of FtsZ polymers into closed rings (cf. ref 8), (ii) the addition of the diffusion of FtsZ into the midcell region, and (iii) the interaction of FtsZ polymers with membrane-binding proteins.

The removal of FtsZ polymer cyclization followed from our recent work to determine the persistence length of FtsZ, i.e., the length scale below which the polymer molecule is essentially straight, which is  $1.15 \pm 0.25 \mu\text{m}$ ,<sup>9</sup> because mature *E. coli* have a circumference of approximately  $2.5 \mu\text{m}$ , *in vivo* FtsZ most

probably forms short linear chains rather than rings curved around the circumference of the cell.

The cell is conceptually divided into three compartments: (1) the cell caps, (2) the midcell region, and (3) the midcell membrane (as shown in Figure 1A). FtsZ molecules within the cell caps and the midcell region undergo polymerization and GTP hydrolysis reactions, as shown in Figure 1B, and transport between these two compartments is by diffusion with rate constant  $k_{dif}$ . Movement occurs from the midcell region to the midcell membrane when FtsZ molecules bind directly to anchor proteins fixed to the membrane or by polymerization reactions to membrane-bound FtsZ. We account for the interaction of single-FtsZ polymers with multiple membrane anchor proteins as depicted in Figure 1C. This depends on the dissociation constant of the FtsZ–anchor interaction ( $\kappa = k_{bind2}/k_{bind1}$ ) and the density of anchor proteins on the membrane. Using the midcell membrane surface area and the number of anchor proteins available, this anchor density is expressed as a probability that a bound FtsZ monomer is adjacent to, and consequently binding to, a binding site,  $P_a$ . As polymer length increases, the number of

anchor connections increases, thereby lowering the probability that the polymer will be released from the membrane. Figure 1D shows the fraction of polymers predicted to be singly bound to the membrane and thereby susceptible to release upon dissociation at the anchor site.

CAM-FF accounts for the physical forces required to deform the cell against its surface tension. We assume that the pinching tension generated on Z-ring contraction depends on (i) the population of FtsZ polymers that accumulated in the Z-ring, (ii) the number of membrane protein–FtsZ interactions, and (iii) the force of this interaction. If the calculated maximal tension of the Z-ring exceeds the tension required to oppose the surface tension at a given radius, then we assume that a “black-box” mechanism will result in contraction of the ring and thus a decrease in the Z-ring and midcell diameter with time; i.e., cell division may proceed (this black box could be a ratchet mechanism driven by thermal fluctuations, possibly assisted by a motor component, or by a conformational change in FtsZ upon GTP hydrolysis). Figure 1E summarizes the key variables in the force model.

The assumptions made in CAM-FF are listed below. For any biological system that is consistent with these assumptions, the model predictions are valid. Brief assessments or justifications are provided in parentheses.

(1) The rate of polymerization of GDP-bound FtsZ is zero. (Although GDP-bound FtsZ has been shown to polymerize, the equilibrium constant is significantly lower than that for GTP<sup>10</sup> and was assumed to equal 0 in the original Surovtsev model.<sup>8</sup>)

(2) GTP hydrolysis occurs within membrane-bound FtsZ polymers in the same way as for free polymers. (This is plausible in the absence of evidence to the contrary.)

(3) The dissociation of the FtsZ polymer following GTP hydrolysis proceeds at a rate  $k_{dis}$  of  $0.075\text{ s}^{-1}$ . (The value of  $k_{cat}$  from Romberg and Mitchison of  $4.5\text{ min}^{-1}$  leads to this value.<sup>11</sup>)

(4) All lengths of the FtsZ polymer diffuse at the same rate. (Failure of this assumption to hold may account in part for the overly rapid assembly of the Z-ring that CAM-FF predicts if, in fact, longer polymers diffuse more slowly than monomers and/or oligomers.)

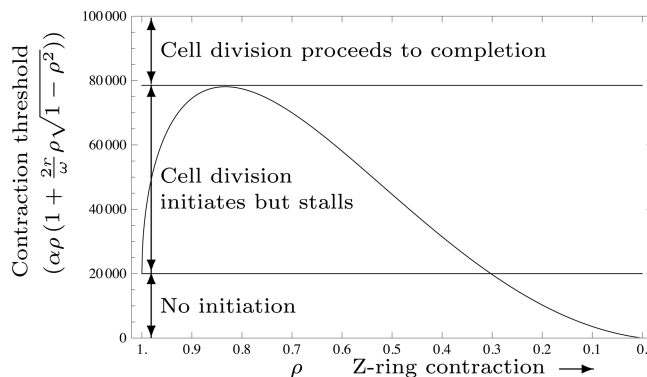
(5) The number of membrane anchor proteins,  $B$ , amounts to 30% of the cell complement of ZipA and FtsA. (Stricker et al. found that at equilibrium, approximately 30% of the cell complement of ZipA was localized to the Z-ring.<sup>12</sup>)

(6) Min and nucleoid occlusion systems were functional, permitting binding of FtsZ polymers in the midcell region only. (This is valid in the wild-type scenario but may not hold in certain mutants.)

(7) FtsZ polymers do not grow longer than a given length. (We verified that increasing the value to  $>150$  subunits does not affect the model output appreciably.)

(8) The initiation threshold value  $\alpha$  is 20000; the wild-type contraction parameter value  $\chi$  is sufficient to allow full division with the capacity to lose 15% of its value before division behavior is affected. (The initiation threshold is set such that the maximal value of the threshold plot as shown in Figure 2, the division completion threshold, CT, is 85% of the wild-type parameter value  $\chi$ .)

(9) The value of  $\chi$  is constant. (We consider this to be reasonable for the initial stages of division that determine the division outcome because the peak of the threshold curve is reached early in the division process since  $\rho = 0.833$ , independent of the value of initiation threshold  $\alpha$ .)



**Figure 2.** Contraction threshold. The contraction threshold is shown as a function of  $\rho$ , the dimensionless ratio of the radius of the Z-ring to the original radius; i.e., contraction proceeds from  $\rho = 1$  to  $\rho = 0$ . Parameter values are as follows:  $\alpha = 20000$ ,  $r = 0.4\ \mu\text{m}$ , and  $\omega = 0.1\ \mu\text{m}$ .

(10) If the calculated maximal tension of the Z-ring exceeds the tension required to oppose the cell surface tension at a given radius, thermal fluctuations will result in contraction of the ring and a decrease in the Z-ring and midcell diameter with time.

## RESULTS

**Model Overview.** In CAM-FF a complex system of biochemical and biophysical interactions is captured by a single index, the contraction parameter,  $\chi$ , which links the population of membrane-bound FtsZ molecules to the force of constriction and can be used to predict the cell’s ability to divide. It is given by

$$\chi = \bar{i}^2 N_z \tag{1}$$

where  $\bar{i}$  is the average number of FtsZ subunits in the membrane-bound polymers and  $N_z$  is the total number of membrane-bound FtsZ polymers. The key result is that, to initiate contraction of the Z-ring, the value of  $\chi$  must exceed the initiation threshold  $\alpha$  that is given by

$$\alpha = \frac{\tau_0 \omega r}{FP_a I_0} \tag{2}$$

where  $\tau_0$  is the cell surface tension,  $\omega$  is the width of the Z-ring,  $r$  is the radius of the Z-ring before contraction,  $F$  is proportional to the force of the interaction of FtsZ with a single membrane anchor site,  $P_a$  represents the surface density of membrane-bound proteins ZipA and FtsA (i.e., the probability that an FtsZ subunit is adjacent to an anchor on the membrane), and  $I_0$  is the length of one FtsZ subunit.

Following initiation, for the Z-ring to continue to contract, the following condition applies:

$$\chi > \alpha \rho \left( 1 + \frac{2r}{\omega} \rho \sqrt{1 - \rho^2} \right) \tag{3}$$

where  $\rho$  is the dimensionless ratio of the radius of the Z-ring at any time point relative to the original radius  $r$ . As contraction proceeds,  $\rho$  decreases from 1 to 0. A plot of the contraction threshold as a function of  $\rho$  is given in Figure 2. Because the contraction parameter  $\chi$  must exceed the contraction threshold at all values of the radius ratio from 1 to 0 for contraction to proceed, three outcomes are possible: (i) division proceeds to completion, (ii) division is initiated but stalls prior to completion, and (iii) division is not initiated.

These outcomes are indicated schematically in Figure 2. The maximal value of the threshold plot can be regarded as the

**Table 1. Model Predictions for Different Cell Characteristics at Kinetic Equilibrium<sup>a</sup>**

	$\bar{l}$	%	$N_z$	$\chi$	$\alpha$	CT	division outcome
wild type	14	28	504	91836	20000	78086	complete
GTP Hydrolysis, WT, $k_{dis} = 0.075 \text{ s}^{-1}$							
0.06 (80%)	15	30	485	112470	20000	78086	complete
0.053 (70%)	16	31	475	125010	20000	78086	complete
0.045 (60%)	18	33	461	142634	20000	78086	complete
0.038 (50%)	19	34	448	161989	20000	78086	complete
0.09 (120%)	12	26	519	76877	20000	78086	initiation only
0.105 (140%)	11	24	531	65671	20000	78086	initiation only
0.12 (160%)	10	22	542	56756	20000	78086	initiation only
0.135 (180%)	9	21	551	49717	20000	78086	initiation only
0.15 (200%)	9	20	559	43987	20000	78086	initiation only
GTP Binding, WT, $k_{ex1} = 0.01 \mu\text{M}^{-1} \text{ s}^{-1}$							
0.008 (80%)	13	27	505	90773	20000	78086	complete
0.006 (60%)	13	27	507	88642	20000	78086	complete
0.005 (50%)	13	27	509	86634	20000	78086	complete
0.004 (40%)	13	26	513	83199	20000	78086	complete
0.003 (30%)	12	26	520	76753	20000	78086	initiation only
0.002 (20%)	11	24	534	63432	20000	78086	initiation only
0.001 (10%)	8	18	572	34802	20000	78086	initiation only
FtsZ Polymerization, WT, $k_{dim1} = k_{el1} = k_{an} = 4 \mu\text{M}^{-1} \text{ s}^{-1}$							
3 (75%)	11	24	528	67721	20000	78086	initiation only
2 (50%)	9	20	559	43097	20000	78086	initiation only
1 (25%)	6	14	603	18867	20000	78086	no initiation
Anchor Deletion							
ZipA, $B = 222, P_a = 0.014$	15	12	504	46978	61429	239836	no initiation
FtsA, $B = 450, P_a = 0.029$	14	21	365	76045	29665	115821	initiation only
FtsZ Overexpression, WT							
$[\text{FtsZ}] = 24 \mu\text{M}$ (200%)	27	42	386	277974	20000	78086	complete
$[\text{FtsZ}] = 36 \mu\text{M}$ (300%)	36	48	328	425000	20000	78086	complete
ZipA Overexpression, WT							
$B = 1122, P_a = 0.072$ (200%)	12	35	741	103349	11944	46633	complete
$B = 1572, P_a = 0.101$ (300%)	10	39	968	96267	8515	33245	complete
<i>ftsZ84</i> Mutation, $k_{ex1} = 3 \times 10^{-4} \mu\text{M}^{-1} \text{ s}^{-1}$							
2:1 ATP:GTP Ratio, $[\text{NTP}] = 270 \mu\text{M}, [\text{NDP}] = 20 \mu\text{M}$							
$k_{dis\_eff} = 0.075 \text{ s}^{-1}$	7	16	584	27328	20000	78086	initiation only
$k_{dis\_eff} = 0.05 \text{ s}^{-1}$	11	24	532	65672	20000	78086	initiation only
$k_{dis\_eff} = 0.042 \text{ s}^{-1}$	13	27	509	88161	20000	78086	complete
3:1 ATP:GTP Ratio, $[\text{NTP}] = 360 \mu\text{M}, [\text{NDP}] = 20 \mu\text{M}$							
$k_{dis\_eff} = 0.075 \text{ s}^{-1}$	8	19	566	38547	20000	78086	initiation only
$k_{dis\_eff} = 0.047 \text{ s}^{-1}$	14	28	505	92914	20000	78086	complete
$k_{dis\_eff} = 0.038 \text{ s}^{-1}$	16	32	477	128136	20000	78086	complete
4:1 ATP:GTP Ratio, $[\text{NTP}] = 450 \mu\text{M}, [\text{NDP}] = 20 \mu\text{M}$							
$k_{dis\_eff} = 0.075 \text{ s}^{-1}$	9	21	553	47945	20000	78086	initiation only
$k_{dis\_eff} = 0.045 \text{ s}^{-1}$	15	30	486	114890	20000	78086	complete
$k_{dis\_eff} = 0.0, k_{dis\_eff} = 0.035 \text{ s}^{-1}$	19	35	455	160818	20000	78086	complete
<i>ftsZ84</i> Recovery, $k_{ex1} = 3 \times 10^{-4} \mu\text{M}^{-1} \text{ s}^{-1}, [\text{NTP}] = 270 \mu\text{M}, [\text{NDP}] = 20 \mu\text{M}, k_{dis\_eff} = 0.075 \text{ s}^{-1}$							
<i>ftsZ84</i> Overexpression							
$[\text{FtsZ84}] = 24 \mu\text{M}$ (200%)	24	41	415	247715	20000	78086	complete
$[\text{FtsZ84}] = 36 \mu\text{M}$ (300%)	80	70	218	1390710	20000	78086	complete
ZipA Overexpression <i>ftsZ84</i>							
$B = 1122, P_a = 0.072$ (200%)	7	24	897	39085	11944	46633	initiation only
$B = 1572, P_a = 0.101$ (300%)	6	27	1215	37631	8515	33245	complete

<sup>a</sup>Unless stated otherwise, all input parameter values are as listed in Table 2. The wild-type input parameter values were used to set the initiation threshold value  $\alpha$  to 20000.  $\bar{l}$  is the average length of membrane-bound FtsZ polymers, % the percentage of FtsZ that is membrane-bound,  $N_z$  the number of membrane-bound FtsZ polymers,  $\chi$  the contraction parameter,  $\alpha$  the initiation threshold, and CT the completion threshold.

division completion threshold. Despite a number of simplifications, CAM-FF makes accurate predictions of cell division behavior.<sup>7</sup> However, the estimates of time scales of the process, while correct in terms of relative ordering, are too short, for

reasons that are discussed below. The model has been implemented in *Mathematica* 8 as detailed in our previous paper.<sup>7</sup> Here we present the predicted wild-type behavior and the predicted effects of various perturbations to key biochemical



parameters and contrast those predictions with available experimental data.

**Wild-Type Model Predictions.** The predicted populations of membrane-bound FtsZ at equilibrium according to CAM-FF are summarized in Table 1. The average bound polymer length ( $\bar{i}$ ), the percentage of the FtsZ population incorporated into the Z-ring, the total number of membrane-bound FtsZ polymers ( $N_z$ ), and the value of  $\chi$  at equilibrium are shown, as well as the predicted division outcome. Using the wild-type parameter values as listed in Table 2, the average membrane-bound polymer

**Table 2. Wild-Type Parameter Values**

parameter	wild-type value	units	ref
$[\text{FtsZ}]_{\text{Total}}$	12	$\mu\text{M}$	Surovtsev et al. <sup>8</sup>
$[\text{GTP}]$	90	$\mu\text{M}$	Surovtsev et al. <sup>8</sup>
$[\text{GDP}]$	10	$\mu\text{M}$	Surovtsev et al. <sup>8</sup>
$B$	672	—	Rueda et al. <sup>23</sup>
$P_a$	0.043	—	Rueda et al., <sup>23</sup> Surovtsev et al. <sup>8</sup>
$\kappa$	0.2	$\mu\text{M}$	Haney et al. <sup>10</sup>
$i_{\text{max}}$	150	—	Surovtsev et al. <sup>8</sup>
$k_{\text{ex1}}$	0.01	$\mu\text{M}^{-1} \text{s}^{-1}$	Mukherjee et al., <sup>52</sup> Chen et al., <sup>53</sup> Surovtsev et al. <sup>8</sup>
$k_{\text{ex2}}$	0.005	$\mu\text{M}^{-1} \text{s}^{-1}$	Mukherjee et al., <sup>52</sup> Chen et al., <sup>53</sup> Surovtsev et al. <sup>8</sup>
$k_{\text{dim1}}$	4	$\mu\text{M}^{-1} \text{s}^{-1}$	Chen et al., <sup>53</sup> Surovtsev et al. <sup>8</sup>
$k_{\text{dim2}}$	40	$\text{s}^{-1}$	Chen et al., <sup>53</sup> Surovtsev et al. <sup>8</sup>
$k_{\text{el1}}$	4	$\mu\text{M}^{-1} \text{s}^{-1}$	Chen et al., <sup>53</sup> Surovtsev et al. <sup>8</sup>
$k_{\text{el2}}$	0.4	$\text{s}^{-1}$	Chen et al., <sup>53</sup> Surovtsev et al. <sup>8</sup>
$k_{\text{an}}$	4	$\mu\text{M}^{-1} \text{s}^{-1}$	Chen et al., <sup>53</sup> Surovtsev et al. <sup>8</sup>
$k_{\text{dis}}$	0.075	$\text{s}^{-1}$	Romberg and Mitchison <sup>11</sup>
$k_{\text{dif}}$	78	$\mu\text{M}^{-3} \text{s}^{-1}$	Culbertson et al. <sup>54</sup>
$k_{\text{bind1}}$	0.142	$\mu\text{M}^{-1} \text{s}^{-1}$	Haney et al., <sup>10</sup> Stricker et al. <sup>12</sup>
$k_{\text{bind2}}$	0.0284	$\text{s}^{-1}$	Haney et al., <sup>10</sup> Stricker et al. <sup>12</sup>

length is predicted to be 14 subunits, with 28% of the cell complement of FtsZ predicted to be membrane-bound at equilibrium. This is in accordance with the values measured experimentally of 30–35%.<sup>12,13</sup>

CAM-FF predicts a Z-ring formation time (5 s) significantly faster than that observed experimentally (1 min),<sup>14,15</sup> which is a consequence of assuming a single diffusion constant for all lengths of FtsZ polymer and of using the rates as measured *in vitro*, without accounting for the inhibitory effect of the cell environment viscosity and crowding (see Experimental Procedures). Accounting for this effect would slow down Z-ring assembly without materially affecting the prediction of cell division outcome. Because insufficient data are currently available to constrain these processes and our main interest is in relative orderings, we retain the simplest assumptions rather than incorporating ad hoc adjustments, accepting an order of magnitude time scale error.

**Measurement of the GTPase Activity of FtsZ Alone Cannot Predict Cell Division.** The experimental observation that an FtsZ mutant has a reduced rate of GTP hydrolysis can be attributed to a number of different causes, including (i) a reduced rate constant of the hydrolysis/dissociation reaction, (ii) a reduced binding efficiency of GTP, or (iii) a reduced rate of FtsZ polymerization, because the GTPase active site is formed at the interface of two FtsZ subunits within the polymer. The same net effect in the cell would be obtained with lower FtsZ or GTP concentrations. The advantage of a mathematical model such as

CAM-FF is these various scenarios can be explored independently.

As summarized in Table 1, a decrease in the rate of GTP hydrolysis/dissociation (with no other concomitant changes) results in increases in the average bound polymer length, the percentage incorporation, and the value of the contraction parameter as well as a decrease in the number of membrane-bound FtsZ polymers. An increase in the rate of GTP hydrolysis has the opposite effects. Because the initiation threshold value  $\alpha$  is by assumption independent of the rate of GTP hydrolysis, eq 2, CAM-FF indicates that a loss-of-GTPase-function mutation in FtsZ does not impair the ability of the cell to initiate contraction and may even render the cell better able to divide as the equilibrium value of the contraction parameter increases. Conversely, an increase in the rate of hydrolysis reduces the ability of the cell to divide.

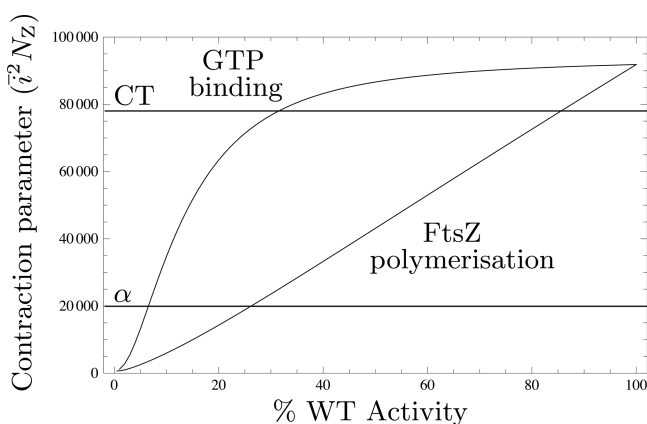
This prediction is corroborated by the behavior of curcumin [1,7-bis(4-hydroxy-3-methoxy-phenyl)hepta-1,6-diene-3,5-dione], an antibacterial phenolic compound that is present in turmeric.<sup>16</sup> Curcumin's effect is to inhibit growth of *E. coli* and *Bacillus subtilis* cell cultures. Its mode of action is via direct binding to FtsZ and disruption of FtsZ polymerization and bundling. The binding of curcumin results in an increase in the rate of GTP turnover and in the rate of FtsZ depolymerization.<sup>16</sup> This may be due to a direct increase in the rate of the GTP hydrolysis reaction, induced by the change in FtsZ secondary structure upon binding of curcumin. Alternatively, the increase in the rate of GTP turnover may be due to a steric hindrance upon polymer bundling (which is not explicitly represented in our model). Such a steric hindrance has the same effect as a direct increase in the GTP hydrolysis/dissociation rate in CAM-FF compared to the wild-type case, because polymer bundling has been shown to decrease the intrinsic rate of GTP hydrolysis by FtsZ.<sup>17</sup> An increase in the GTP hydrolysis/dissociation rate constant in CAM-FF reduces  $\chi$  and inhibits cell division. A mechanism with an increased rate of GTP turnover may also deplete the cell's supply of GTP, which further reduces the degree of accumulation of FtsZ polymers.

If taken to its logical conclusion, the effect of an extreme reduction in the intrinsic hydrolysis rate, all else being equal, would seem to be that cell division is maximally expedited (i.e., maximal cell division when there is no GTPase activity). However, this overlooks the fact that a reduced level of hydrolysis also results in the accumulation of longer polymers. Given the persistence length of FtsZ,  $\sim 1 \mu\text{m}$ ,<sup>9</sup> such accumulation will impede cell division. Moreover, while a reduced level of GTP hydrolysis promotes Z-ring formation, the Z-ring must depolymerise later in the cycle and a complete loss of GTPase activity would arrest this process. It is unlikely that an extreme perturbation to the hydrolysis rate could arise without some accompanying effect on GTP binding and FtsZ polymerization.

The analysis suggests a possible function of FtsZ-interacting protein ZapA. It has been clear for some time that ZapA slows GTP hydrolysis when ZapA is added to FtsZ *in vitro*.<sup>18,19</sup> At a ZapA:FtsZ mixing ratio of 4:1, the GTPase activity is reduced by  $\sim 50\%$ .<sup>19</sup> However, the mechanism of slowing remains unclear. Our analysis suggests that by reducing the rate of GTP hydrolysis, ZapA promotes the formation of longer polymers and reduces the time taken for the cell to reach the critical contraction threshold, thus accelerating cell division once Z-ring formation has started.

As summarized in Table 1, either reduced GTP binding strengths or reduced FtsZ polymerization rates lead to the

formation of shorter polymers. These factors inhibit the formation of the Z-ring and weaken its contraction ability, which is similar to the effect of increasing the GTPase activity of FtsZ. Expression of the reduction of activity as a percentage of the wild-type value allows a direct comparison. Although a significant reduction of the rate of GTP binding can adversely affect cell division, CAM-FF suggests that the effect is relatively small, so competitive inhibition of binding of GTP to FtsZ would be an ineffective strategy for the development of targeted antibacterial drugs (Figure 3).



**Figure 3.** Drug targeting: GTP binding vs FtsZ polymerization. Decreasing the rate of FtsZ polymerization is a more efficient approach to prevention of cell division than inhibition of GTP binding. The initiation ( $\alpha$ ) and completion (CT) thresholds are shown. All other parameter values are as listed in Table 2.

The predicted modest effect of a reduction in the rate of GTP binding may explain why C8-substituted guanine, guanosine, guanosine 5'-monophosphate (GMP), and guanosine 5'-triphosphates have been found to be ineffective antibacterial agents against *E. coli*, despite the C8-substituted GTP analogues displaying strong inhibition of FtsZ polymerization *in vitro*<sup>20,21</sup> by competition for the GTP-binding site. It should be noted that the lack of toxicity was not due to a low level of intracellular accumulation or the absence of conversion of the analogue to the inhibitory triphosphate form.<sup>20</sup>

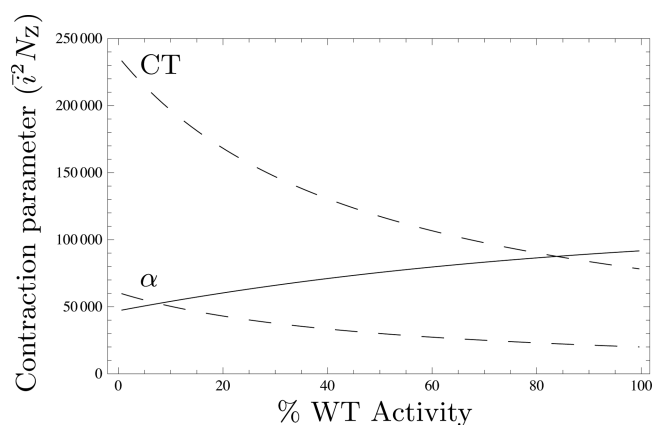
Compared with inhibition of GTP binding, reduction of FtsZ polymerization affects the contraction parameter more strongly and so would be predicted to be a more effective approach to arresting cell division. The differential change of  $\chi$ , with respect to a change in the input parameter, gives a quantitative measure of the sensitivity of the system to perturbation of a specific biochemical interaction. To express the sensitivity as a dimensionless measure, which allows direct comparison of the different input parameters, we use a sensitivity coefficient given by  $p\Delta\chi/(\chi\Delta p)$  as a relative measure, where  $p$  is the value of the parameter. For example, for the GTP binding constant, using the value of  $\chi$  obtained for the parameter values of 99% of the wild-type GTP binding rate constant ( $p = 0.0099 \mu\text{M}^{-1} \text{s}^{-1}$ ;  $\chi = 91,796$ ) and 101% of the wild-type GTP binding rate constant ( $p = 0.0101 \mu\text{M}^{-1} \text{s}^{-1}$ ;  $\chi = 91,874.7$ ) to approximate the sensitivity of the wild-type system to changes to the rate of GTP binding, the sensitivity coefficient is given by  $(0.01 \times 78.7)/(91835.9 \times 0.0002) = 0.043$ . By comparison, the sensitivity coefficient for FtsZ polymerization is 1.035, which indicates that rational drug design effort should be focused on the FtsZ–FtsZ interaction rather than on the inhibition of GTP binding. Indeed, Duggirala

et al. recently reported the inhibitory effect of coumarin derivatives on *B. subtilis* growth with inhibition of FtsZ polymerization observed *in vitro*.<sup>22</sup> *In silico* docking studies suggested the inhibitory effect was due to binding of coumarin to residues of the T7 loop of FtsZ. This prevented FtsZ polymerization by targeting the C-terminal end of the molecule, rather than via competitive inhibition of GTP binding at the N-terminal domain.

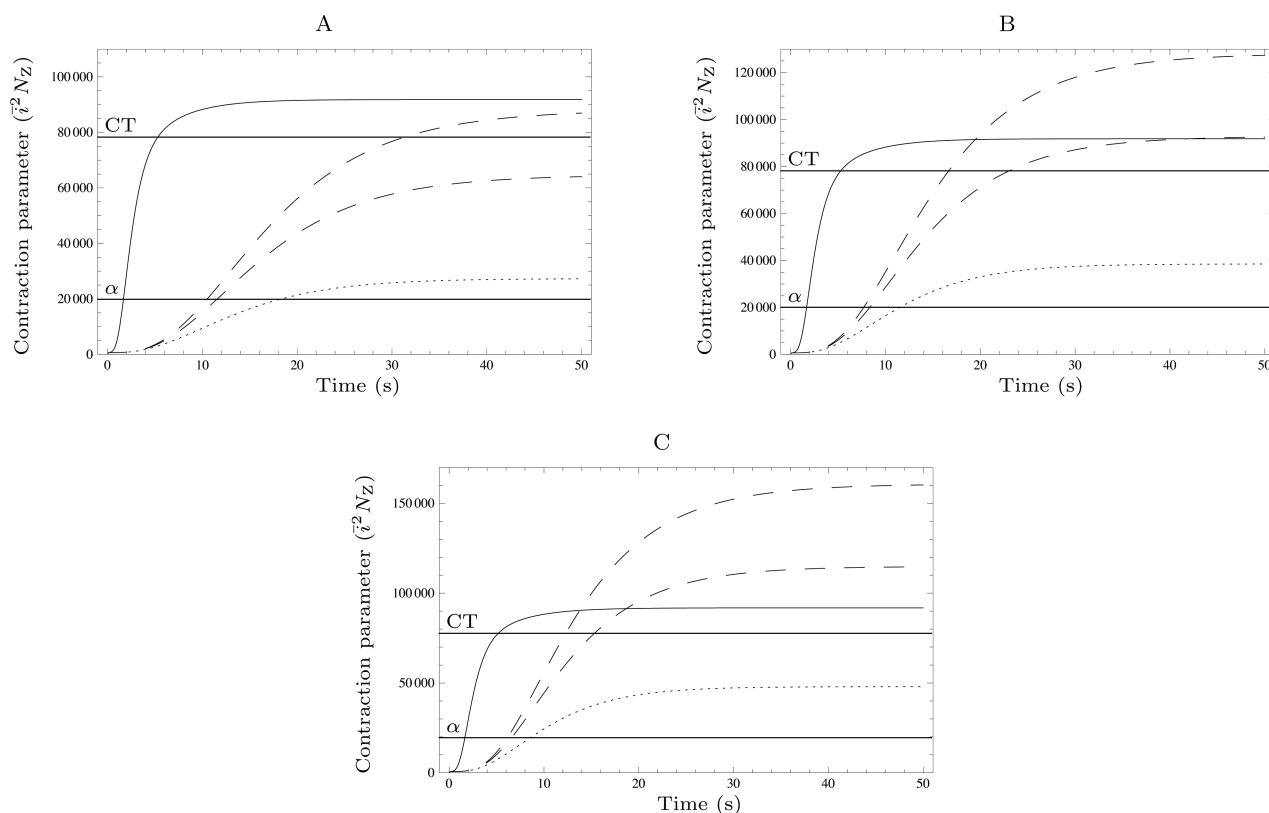
**Predicting the Effect of Anchor Protein Deletion.** In CAM-FF, it is assumed that ZipA and FtsA have equivalent effects in anchoring FtsZ to the membrane and the total number of anchor proteins is given by the parameter  $B$ . The experimental literature cites the numbers of molecules per cell for ZipA and FtsA as 1500 and 740, respectively,<sup>23</sup> and according to Stricker et al.,<sup>12</sup> approximately 30% of the cell complement of ZipA localizes to the Z-ring *in vivo*. We used a wild-type value for  $B$  of 672 when we assumed that 30% of the cell complement of anchor proteins is located at the midcell.

The effect of removing the contribution from either ZipA or FtsA (mimicking a deletion mutant) is summarized in Table 1. Upon deletion of ZipA,  $P_a$  is reduced by 67%, corresponding to a total number of anchor proteins of 740 (FtsA only), with 30% located on the midcell membrane to give the number of membrane anchor proteins ( $B = 222$ ). The consequence is that the initiation threshold increases substantially so cells are predicted to be unable to initiate contraction in the absence of ZipA. This prediction is corroborated by the experimental observation that ZipA is essential for cell division to occur, even though the Z-ring does form in the absence of ZipA.<sup>24</sup> Thus, CAM-FF accurately predicts the outcome of ZipA depletion.

The lack of division of a ZipA deletion mutant might suggest ZipA as an antibiotic target. However, the development of small molecule inhibitors has met with limited success. Targeting protein–protein interactions with small molecules remains a challenge because of the relatively large interaction area of the ZipA–FtsZ protein surfaces.<sup>25</sup> Inhibitors discovered by screening<sup>26</sup> and computational methods<sup>27</sup> often have affinities that are too low for therapeutic use but provide lead compounds for development. Figure 4 shows the equilibrium value of the contraction parameter for reductions of the number of ZipA available for FtsZ–membrane anchoring. Between approximately 5 and 85% of the wild-type level of ZipA availability, cells



**Figure 4.** Drug targeting of ZipA. Decreasing the number of ZipA-binding sites available (solid line) is an effective approach to the prevention of cell division. The initiation ( $\alpha$ ) and completion (CT) thresholds are shown (dashed lines). All other parameter values are as listed in Table 2.



**Figure 5.** ATP binding and hydrolysis by the *ftsZ84* temperature-sensitive mutant. The solid line shows data for the wild-type solution. For all other plots,  $k_{\text{ext}} = 3 \times 10^{-4} \mu\text{M}^{-1} \text{s}^{-1}$ . For the dotted line, at 42 °C,  $k_{\text{dis, eff}} = 0.075 \text{s}^{-1}$ . Dashed lines correspond to reduced temperatures: (short dashes) a 2-fold decrease in the rate of ATP hydrolysis and (long dashes) a 3-fold decrease in the rate of ATP hydrolysis. (A) ATP:GTP ratio of 2:1, [NTP] = 270  $\mu\text{M}$ , [NDP] = 20  $\mu\text{M}$ . (B) ATP:GTP ratio of 3:1, [NTP] = 360  $\mu\text{M}$ , [NDP] = 20  $\mu\text{M}$ . (C) ATP:GTP ratio of 4:1, [NTP] = 450  $\mu\text{M}$ , [NDP] = 20  $\mu\text{M}$ . All other parameters as listed in Table 2. The initiation ( $\alpha$ ) and completion (CT) thresholds are shown.

are able to initiate division, but contraction will stall prior to completion. Conversely, for an increase in the level of expression of ZipA, the average membrane-bound polymer length is fairly stable, whereas the percentage incorporation increases, as does the number of membrane-bound FtsZ polymers, so cell division is facilitated. The sensitivity coefficient for the effect of the number of ZipA-binding sites available on the value of contraction parameter  $\chi$  is 0.204.

Upon deletion of less abundant FtsA,  $P_a$  is reduced by 33% (corresponding to a total number of anchor proteins of 1500). CAM-FF predicts that  $\chi$  reaches the initiation threshold but that contraction stalls prior to completion. This is consistent with observations that FtsA-depleted cells exhibit indentations above the Z-ring, indicating that contraction is initiated, but division does not occur.<sup>24</sup> ZipA-depleted cells (discussed above), by contrast, appear completely smooth,<sup>24</sup> indicating that contraction is not even being initiated.

**Overexpression of FtsZ.** If FtsZ is overexpressed, CAM-FF predicts increases of the average bound polymer length and the percentage incorporation of FtsZ into the Z-ring, but a decrease in the number of bound FtsZ polymers. The  $\chi$  value indicates that the cells are better able to divide than the wild type. However, FtsZ overexpression also affects assumption 6 [the confinement of membrane-bound FtsZ polymers to the midcell by the Min system (see Experimental Procedures)], which is no longer valid: membrane-bound FtsZ will also be found at the cell poles. For example, at 2.7-fold overexpression of FtsZ in *E. coli*, the “minicell phenotype” is induced, in which divisions occur at the cell poles, in addition to the normal midcell divisions. As a closely

similar phenotype follows deletion of the Min operon, it appears reasonable to suppose that control by the Min system is overwhelmed at increased concentrations of FtsZ. Furthermore, because the function of MinC is to antagonize the polymerization activity of FtsZ,<sup>28</sup> the phenotype observed upon loss of intrinsic GTPase activity in FtsZ, which promotes polymerization, somewhat resembles the loss of the Min system. In FtsZ overexpression studies, it was found that once the concentration of FtsZ reaches 12 times the wild-type value, all divisions are inhibited and cells become filamentous.<sup>29</sup>

The predicted average membrane-bound polymer length of 36 subunits for 3-fold FtsZ overexpression corresponds to an average polymer length of  $\sim 0.14 \mu\text{m}$ , which is on the order of magnitude of the cell radius. In view of the persistence length of FtsZ,<sup>9</sup> such long polymers are not thought to occur in *E. coli* as they would not bend to form the Z-ring. The behavior of FtsZ when assumption 6 breaks down has not yet been built into the model.

**Temperature Sensitivity of the *ftsZ84* Mutation.** The GTPase activity of the FtsZ84 (FtsZ-G105S) mutant protein is approximately one-tenth of that of the wild-type protein, because of its strongly reduced affinity for GTP.<sup>30</sup> So far, it has not been clear why cells bearing the *ftsZ84* mutation appear to divide normally at 30 °C but are unable to divide at 42 °C, particularly because the GTPase activity appears to be temperature-insensitive over this range.<sup>30,31</sup> Translation of the activity of the FtsZ84 protein measured *in vitro* into CAM-FF parameters allows us to explore the biochemical mechanism underlying this temperature sensitivity.



According to RayChaudhuri and Park, the FtsZ84 mutant protein also catalyzes the hydrolysis of ATP, a function not present in the wild-type protein.<sup>31</sup> Filter retention assays with radiolabeled nucleotides showed that the binding affinity of the mutant protein for ATP is approximately 30 times lower than the affinity of the wild-type protein for GTP.<sup>31</sup> The concentration of nucleotides within the cell is known to vary with growth conditions,<sup>32,33</sup> but according to Bennett et al., in *E. coli* the concentration of ATP is approximately twice that of GTP and the concentrations of ADP and GDP are approximately equal.<sup>34</sup> At 42 °C, the mutant has a similar level of ATPase and GTPase activity, whereas at 30 °C, the ATPase activity is a third of that of the GTPase.<sup>31</sup>

To model the behavior of *ftsZ84*, we applied a 30-fold reduction in the rate of nucleotide triphosphate (NTP) binding, as well as a range of different increases in the concentration of the pool of activating nucleotides (because the measured concentrations of ATP vary), as indicated in Table 1, and different ranges of NTPase rates of the FtsZ84 protein to account for changes in the ATPase activity as a function of temperature. We assumed that the binding affinities and rates of polymerization of FtsZ84 are equal for the ATP- and GTP-bound proteins and not temperature-sensitive. These assumptions imply that the proportions of active sites in the ATP- and GTP-bound states correspond to the relative concentrations of ATP and GTP in the nucleotide pool. In view of the linearity of the rate terms in the kinetic equations, we can use a weighted average of the hydrolysis/dissociation rate constants as the effective rate constant  $k_{\text{dis-eff}}$  based on the relative concentrations of the two activating nucleotides. For example, with an ATP:GTP ratio of 2:1 and a 2-fold reduction in the rate of ATP hydrolysis, the effective NTPase rate is  $0.05 \text{ s}^{-1} (2/3 \times 0.0375 + 1/3 \times 0.075 \text{ s}^{-1})$ .

Thus, as summarized in Table 1 and shown in Figure 5, at 42 °C we predict a reduction in the average length of the membrane-bound FtsZ polymers. This in turn results in a dramatic lowering of  $\chi$ . The percentage of FtsZ that is membrane-bound is also reduced. CAM-FF therefore predicts that cell division is initiated but stalls prior to completion at 42 °C. However, for the lower efficiency of the ATPase activity at 30 °C,  $\chi$  increases above the completion threshold in all ATP:GTP ratios but with a 3-fold reduction in activity relative to that of the wild type.

In summary, CAM-FF predicts that cell division occurs at lower temperatures because of the reduction in the ATPase activity of the mutant FtsZ84 protein. The precise point at which the division thresholds are no longer reached depends on the relative concentrations of nucleotides and the true intrinsic rates of hydrolysis/dissociation. The solutions shown in Figure 5 are based on current experimental estimates of the parameters; it is hoped they are representative of a biologically relevant scenario. CAM-FF also predicts that the introduction of a second mutation into the *ftsZ84* gene that reduces the intrinsic rate of hydrolysis, such as “T7 synergy loop” mutations, would restore cell division behavior at the currently nonpermissive temperature.

Furthermore, CAM-FF predicts that an increase in the concentration of FtsZ would restore cell division. Indeed, it has been shown that the introduction, at low copy numbers, of a plasmid containing the *ftsQ*, *ftsA*, and *ftsZ84* genes leads to recovery of cell division in *ftsZ84* cells, but the introduction of the same plasmid with *ftsQ* and *ftsA* only did not restore division.<sup>35</sup> These findings suggest that the recovery effect is due to increased levels of the FtsZ84 protein.

In summary, CAM-FF predicts that the average bound polymer length is 24 subunits for a 2-fold increase in FtsZ84

concentration and 80 subunits for a 3-fold increase. However, as was the case for wild-type FtsZ overexpression, excess expression of FtsZ threatens to invalidate a key assumption of CAM-FF. The possible breakdown of assumption 6 ties in with the experimental observation that introduction of a high-copy number plasmid to *ftsZ84* cells results in the inhibition of cell division as the Min and nucleoid occlusion systems are overwhelmed and membrane binding is no longer restricted to the midcell.<sup>35</sup>

Division activity in *ftsZ84* is restored by increased gene dosage of ZipA at the nonpermissive temperature,<sup>36</sup> in agreement with the simulation results summarized in Table 1. An increase in the number of membrane anchor proteins decreases the threshold value  $\alpha$  and has a small effect on  $\chi$ . With the value of wild-type threshold  $\alpha$  as described above and the number of ZipA molecules per cell increased 3-fold, CAM-FF predicts that the completion threshold is reached and the cell is able to initiate division.

### The Effect of the *ftsZ84* Mutation on Z-Ring Turnover Is Less Pronounced Than Previously Measured.

Two key parameters in CAM-FF are the rate constants for membrane association ( $k_{\text{bind1}}$ ) and dissociation ( $k_{\text{bind2}}$ ) of FtsZ. Because these values are not available, we estimated them from the equilibrium binding constant for the FtsZ–ZipA interaction ( $\kappa = 2 \mu\text{M}$ )<sup>10</sup> and measurements of the half-life of fluorescence recovery (30 s)<sup>12</sup> when membrane-bound FtsZ–GFP is photo-bleached. The observed off rate in the FRAP experiment corresponds to  $k_{\text{bind2}}$  multiplied by  $p_1(\bar{i})$ , the fraction of polymers in the singly bound state ( $p_1$ ) for the average polymer length at equilibrium ( $\bar{i}$ ). Figure 1D shows how the fraction of polymers in the singly bound state decreases for longer polymers (because more FtsZ–anchor interactions keep the FtsZ polymer at the membrane). Cell conditions that increase the average polymer length lead to a decrease in  $p_1(\bar{i})$  and therefore lower the rate of release from the membrane and increase the fluorescence recovery time as  $k_{\text{bind2}}$  is constant. It is therefore predicted that a decrease in the intrinsic rate of GTP hydrolysis, which increases the average polymer length, will lead to an increase in the half-life of recovery.

On the assumption that the constants determined from WT data apply to the *ftsZ84* mutant, CAM-FF predicts only a minor increase in the half-life of recovery for the *ftsZ84* mutant at the permissive temperature: 30 s for an ATP:GTP ratio of 2:1, 32 s for a ratio of 3:1, and 33 s for a ratio of 4:1. This is in contrast to the large increase observed by Stricker et al. and Anderson et al.<sup>12,13</sup> A minor increase in the percentage incorporation of FtsZ into the ring is also observed. However, this increase is considerably smaller than the values of up to ~65% that were reported by Stricker et al.<sup>12</sup> This discrepancy could be due to the fact that different growth conditions were used in their experiments, which affects the values of the rates of NTP hydrolysis as well as the concentrations of available nucleotides and of FtsZ.<sup>33</sup>

## DISCUSSION

A simulation model of cytokinesis that includes kinetics and midcell membrane binding and contraction allows us to generate predictions of the *in vivo* properties of the Z-ring such as the average bound polymer length, the percentage of incorporation of FtsZ into the Z-ring, and whether a cell will initiate and/or complete cytokinesis. Our predictions are in accordance with experimental data, leading us to believe that the model, critical accumulation of membrane-bound FtsZ fibers (CAM-FF),



adequately captures the dynamics of the processes occurring *in vivo*. The key output of CAM-FF is contraction parameter  $\chi$ , which links the force of Z-ring contraction to the dynamics of the intracellular population of membrane-bound FtsZ. This  $\chi$  value is to be compared to threshold values for initiation and completion to predict a cell division outcome. Interrogation of CAM-FF yields insights into the underlying mechanistic basis for observed behaviors. In the case of the *ftsZ84* mutation, model analysis suggests that the loss of division behavior at 42 °C is due to the ATPase activity acquired by the mutant FtsZ protein that increases the concentration of the pool of activating nucleotides (GTP and ATP). However, at lower temperatures where the ATPase activity is reduced, a functional Z-ring is able to form and contract. Moreover, the low turnover rate observed for the FtsZ84 ring *in vivo* may reflect changes in experimental conditions rather than be a true effect of the mutation.

While the explanation of the temperature sensitivity of the *ftsZ84* mutant addresses some of the questions around cell division and cell behavior observed in the laboratory, the key goal of our model is to understand bacterial cell division sufficiently well to determine which components pose the most effective targets for antibacterial agents. Our analysis suggests that targeting the binding of GTP to FtsZ using a competitive inhibitor is an inefficient method of blocking cell division. By contrast, targeting the polymerization of FtsZ or the availability of ZipA- or FtsA-binding sites was shown to be considerably more effective. In summary, CAM-FF predicts the following order of efficiency of the possible drug targets: FtsZ polymerization > ZipA/FtsA availability > GTP binding.

The model predicts which of three division outcomes prevails as a function of parameter values. In those cases where the model predicts that division can initiate but not complete, the filamentous phenotype is observed in the laboratory. The predicted cell phenotype is an important consideration in antibiotic development. Whereas induction of the filamentous phenotype leads to cell lysis following treatment with  $\beta$ -lactam antibiotics such as cephalexin,<sup>37,38</sup> induction of the filamentous phenotype has also been shown to inhibit phagocytosis by macrophages, where access to the filament pole was a crucial factor.<sup>39</sup> Furthermore, the filamentation process is thought to contribute to bacterial virulence in infections of *Legionella pneumophila* (legionnaires' disease),<sup>39</sup> *E. coli* (urinary tract infection),<sup>40</sup> and *Salmonella* (food poisoning).<sup>37</sup> The possibility of inducing dormant states such as those found in *Mycobacterium tuberculosis* infection, in which the organism survives in filamentous form within macrophages,<sup>41</sup> may constitute a form of evasion of host defenses. Moreover, pools of dormant filamentous cells may reinitiate division upon removal of the antibiotic. This has been described as a "negative post-antibiotic effect", where the rate of growth of the bacteria is rapid after the removal of an antibiotic as the filamentous cells simultaneously divide.<sup>42</sup> Indirect evidence of this hypothesis is provided by the phenomenon of a resurgence of urinary tract infection following withdrawal of antibiotics.<sup>40</sup>

The CAM-FF model makes no assumptions about the molecular mechanism of Z-ring contraction and requires only that some minimal force be required for contraction, perhaps generated by a conformational switch in FtsZ itself on GTP hydrolysis,<sup>43–45</sup> which depends on the interaction of FtsZ polymers with the membrane, where the pulling force on the membrane is considered to be proportional to the number of membrane interactions. To the best of our knowledge, no motor protein has yet been found to associate with FtsZ, and it is

conceivable that contraction might proceed without the intervention of such a motor, by means of a nonequilibrium process involving the continual binding and release of FtsZ polymers, depending on the rate of GTP hydrolysis. The release and rebinding of FtsZ polymers in the Z-ring would effectively create a ratchet mechanism whereby local fluctuations become locked in place by the adjacent binding of further FtsZ polymers. Multiple membrane anchors may play a role in the ratchet; e.g., ZipA is tightly anchored within the membrane, whereas FtsA is more weakly bound and so is readily released and rebound during thermal fluctuations of the Z-ring or the cell membrane. Interestingly, FtsA is an ATPase,<sup>46</sup> which suggests a possible means of chemical coupling to drive unidirectional contraction. The state of the bound nucleotide may affect the interaction of FtsA with FtsZ or the cell membrane or both.

An additional role of the Z-ring that is not included in the model is the recruitment of peptidoglycan remodeling enzymes on the outside of the inner cell membrane.<sup>47</sup> As the Z-ring contracts, the peptidoglycan remodeling process creates a physical barrier to any subsequent re-expansion of the Z-ring, which consolidates the progress made thus far and acts as another ratchet. The contribution of the cell wall to division will be considered in future modeling studies. Furthermore, as described in assumption 6 in Experimental Procedures, in CAM-FF the Min and nucleoid occlusion systems are captured in a simplified form by permitting binding of FtsZ to the ZipA/FtsA at the midcell only. This assumption limits CAM-FF to consideration of the effectiveness of inhibitors of the system such as inhibition of GTP binding and FtsZ polymerization, and activation of the GTPase activity of FtsZ. For factors that promote FtsZ polymerization, CAM-FF requires extension to include the factors that validate assumption 6. For example, the antibacterial benzamide PC190723 has been reported as a promoter of FtsZ polymerization in *Staphylococcus aureus*<sup>48–50</sup> and multiple FtsZ rings and arcs are observed in PC190723-treated Methicillin-Resistant *S. aureus*.<sup>51</sup> While CAM-FF in its current form provides insight into various inhibitors of polymerization, those factors that promote polymerization require explicit consideration of the Min and nucleoid occlusion systems.

In conclusion, although certain aspects of the biological process have been simplified in our model and the molecular mechanism of the contraction process remains to be elucidated, analysis of the contraction parameter already allows us to make organism level predictions based on the biochemical activity of FtsZ measured *in vitro*. The model simulations present a relatively cost-effective way of generating novel biological ideas, e.g., the biochemical mechanism of temperature sensitivity of *ftsZ84*. This is particularly important for FtsZ because specific small molecule inhibitors, commonplace in the laboratory for the study of the structural FtsZ homologue tubulin, are absent. This lack limits the study of the effect of loss of a particular function of FtsZ experimentally. The search for potential drug interactions may be aided by evaluation of target efficacy *in silico*.

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## Notes

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## ■ ABBREVIATIONS

CAM-FF, critical accumulation of membrane-bound FtsZ fibers; GDP, guanosine 5'-diphosphate; GMP, guanosine 5'-monophosphate; GTP, guanosine 5'-triphosphate.

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